## Assignment 6

Due date: Friday, October 8

## Electrical resistance between concentric cylinders

Two concentric metal cylinders are placed in an electrolyte solution. When a potential difference $V$ is applied to the two cylinders with a battery, a current $I$ flows from one cylinder to the other. Calculate the resistance $R=V / I$ in terms of the resistivity $\rho$ of the electrolyte and the geometry of the cylinders. Model the cylinders as thin sheets with length $L$ along their common axis and radius $a$ (inner) and $b$ (outer). You may assume that $L \gg b>a$ so that "end effects" can be neglected (the electric field and potential can be approximated by a model with $L=\infty$ ). Also assume that the resistivity of the metal sheets is so small (compared with the electrolyte) that the electric potential is a constant on each cylinder.
Hints: A potential function with cylindrical symmetry is $\varphi(r)=A \log r$, where $A$ is a constant and $r$ is the distance from the cylinder axis. Check this fact by working out the corresponding electric field and comparing with the electric field produced by uniform charge along a line. Use the function $\varphi(r)$ to find the potential difference $V$. From the corresponding electric field at $r=a$ and $r=b$ find the current $I$ that flows into one cylinder and out of the other (they better be the same!).

## A compound resistor

Two cylinders of different semiconducting materials are joined end-to-end to form a compound resistor. Both cylinders have the same cross sectional shape and area $A$. However, the cylinders have different lengths and resistivities: $L_{1}, \rho_{1}$ and $L_{2}, \rho_{2}$. The following parts are not meant to be done in a particular order:

- Find the ratio of electric fields in the two semiconductors, $E_{1} / E_{2}$, when a potential difference is applied between the ends of the compound resistor.
- Find the ratio of potential differences between the ends of the individual semiconductors, $V_{1} / V_{2}$, when a potential difference is applied between the ends of the compound resistor.
- Find the current $I$ that flows along the compound resistor when the potential difference between its ends is $V$.
- Explain why in general a surface charge density $\sigma$ forms where the cylinders are joined and there is a nonzero potential $V$ between the ends of the compound resistor. Calculate the value of $\sigma$.

