

Lecture 3

Suppose the oscillator at $x=0$ is fixed at $\theta=0$ for all times:

$$\theta(0, t) = 0 \quad \underline{\text{all } t}$$

$$f(0-vt) + g(0+vt) = 0 \quad (*)$$

$vt = y$ (a position)

$$(*) \Rightarrow g(y) = -f(-y) \quad \underline{\text{all } y}$$

$$\Rightarrow \theta(x, t) = f(x-vt) + \underbrace{g(x+vt)}_{-f(-x-vt)}$$

general solution with zero boundary condition at $x=0$:

$$\theta(x, t) = f(x-vt) - f(-x-vt)$$

Next, suppose the oscillator at $x=L$ is also fixed at $\theta=0$: (3.2)

$$\theta(L,t) = 0 = f(L-vt) - f(-L-vt)$$

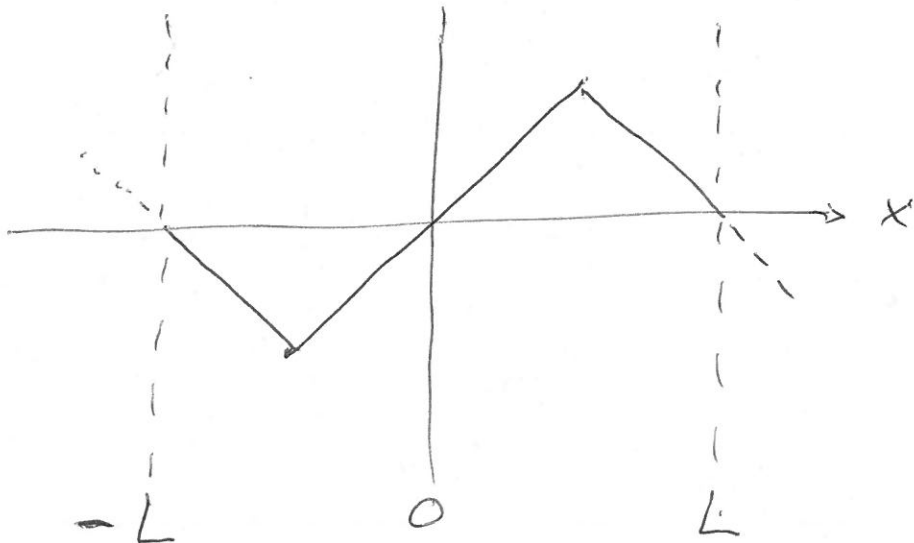
for all t

introduce $y = L - vt$:

$$f(y) = f(y - 2L) \quad \underline{\text{all } y}$$

f is periodic with period $2L$

Example: $f = Z$ "periodic zig-zag"

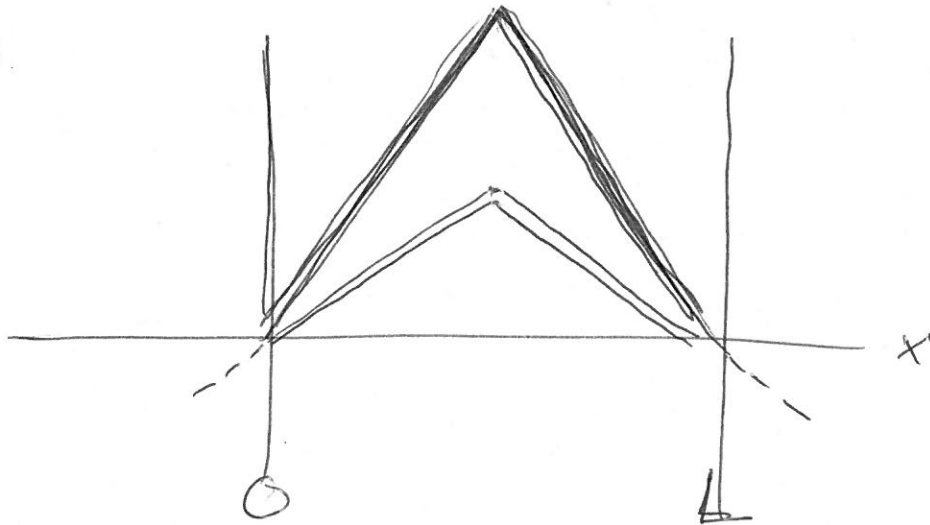


Since $Z(-x) = -Z(x)$, $g(x) = f(x)$

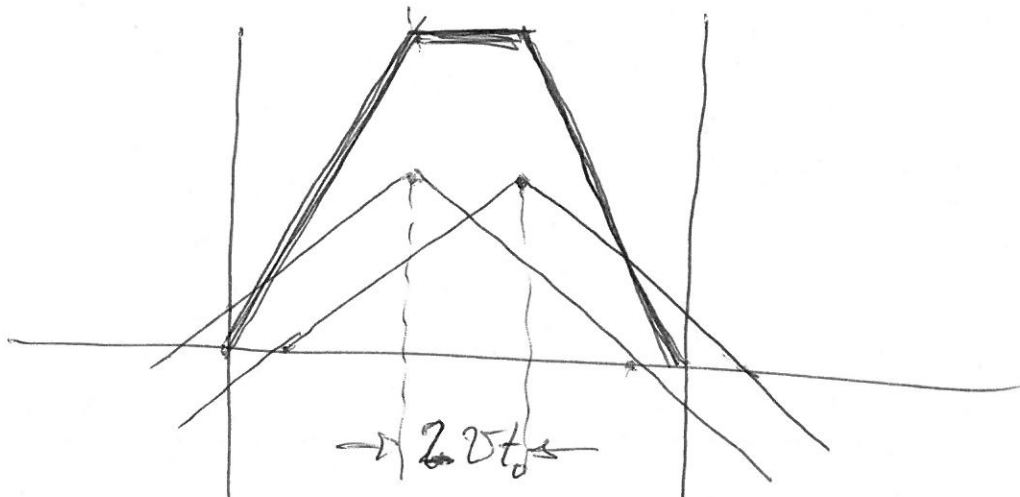
(3.3)

$$\Theta(x, t) = Z(x - vt) + Z(x + vt)$$

$\Theta(x, 0)$



$\Theta(x, t_0)$



$\Theta(x, t_1)$

$$vt_1 = \frac{L}{2}$$

